

**Title/Number:**  
**DSP ECE 623**

by  
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**Lecture 20**  
**Introduction to Special types of**  
**Digital Filters**

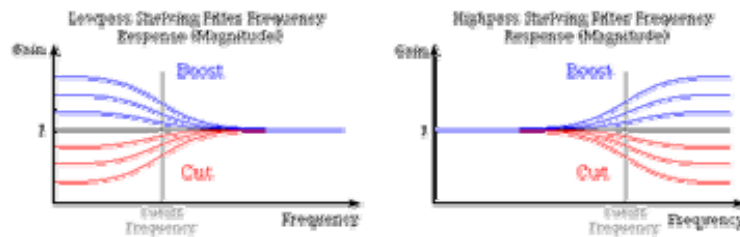
- Shelving Filter
- Peaking Filter
- Graphic Equalizer

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# Shelving Filter

Shelving filters realize tone controls in audio systems. The frequency response of a low-pass (bass) and high-pass (treble) shelving filter is shown below.



Frequency response of a low-pass and high-pass shelving filter.

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The transfer function of low-pass shelving filter is implemented as:

$$H(z) = 1 + (\mu - 1) \frac{\alpha(1 + z^{-1})}{1 - \gamma \cdot z^{-1}}$$

The coefficients  $\mu, \alpha, \gamma$  are related to the cutoff frequency  $f_c$  and the shelving filter boost/cut gain in dB is

$$\gamma = \frac{1 - (4/(1 + \mu)) \tan(\Omega_c/2)}{1 + (4/(1 + \mu)) \tan(\Omega_c/2)}$$

$$\alpha = (1 - \gamma)/2$$

where  $\Omega_c = 2\pi f_c/f_s$ ,

The pole of low-pass shelving filter is calculated by:

$$p = \frac{1 - (4/(1 + \mu)) \tan(\Omega_c/2)}{1 + (4/(1 + \mu)) \tan(\Omega_c/2)}$$

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The transfer function of high-pass shelving filter is implemented as:

$$H(z) = 1 + (\mu - 1) \frac{\alpha(1 - z^{-1})}{1 - \gamma \cdot z^{-1}}$$

where

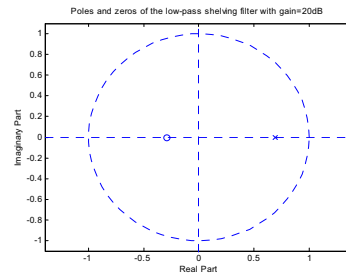
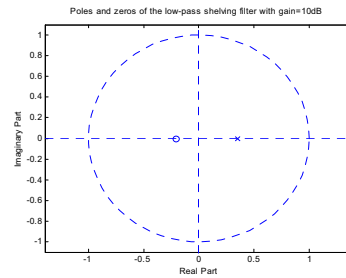
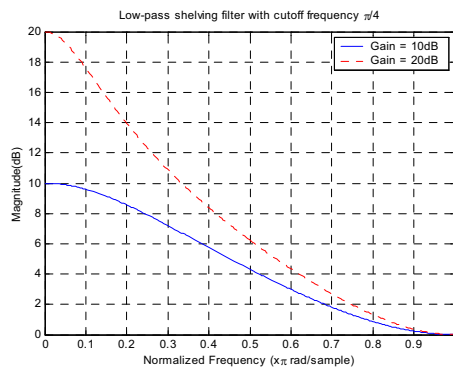
$$\gamma = \frac{1 - ((1 + \mu)/4) \tan(\theta_c/2)}{1 + ((1 + \mu)/4) \tan(\theta_c/2)}$$

$$\alpha = (1 + \gamma)/2$$

The pole of high-pass shelving filter is calculated by:

$$p = \frac{1 - ((1 + \mu)/4) \tan(\theta_c/2)}{1 + ((1 + \mu)/4) \tan(\theta_c/2)}$$

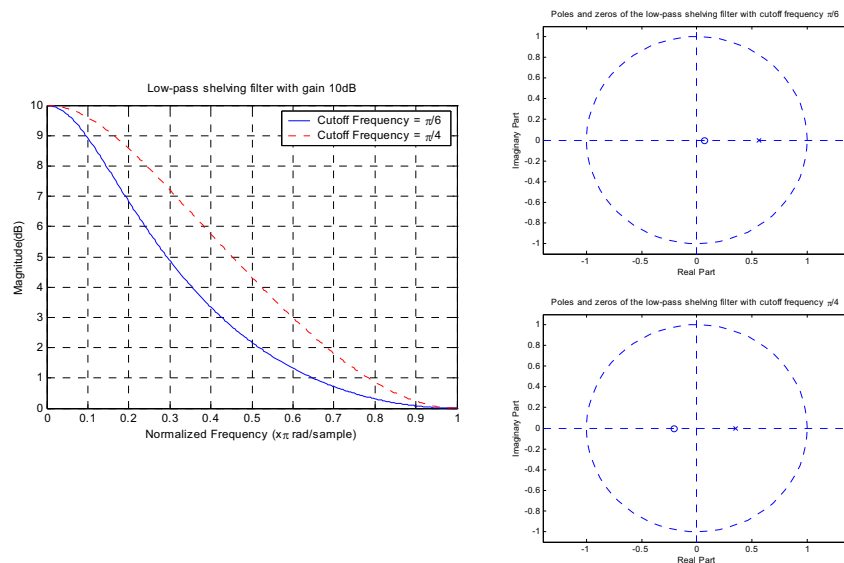
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Frequency response and pole-zero plot of the low-pass shelving filters with different gains.

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Frequency response and pole-zero plot of the low-pass shelving filters with different cutoff frequency . Copyright (c) Andreas Spanias Ch 5-7

## Tone Control Block in J-DSP

The low frequencies are affected by bass adjustments with the audio signal processed through low-pass shelving filters. The high frequencies are affected by treble adjustments with the audio signal processed through high-pass shelving filters. A J-DSP simulation using the Tone Control .

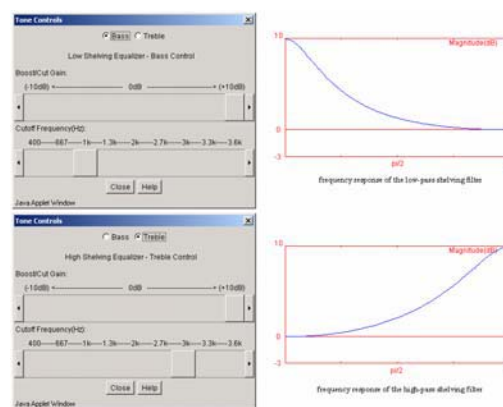


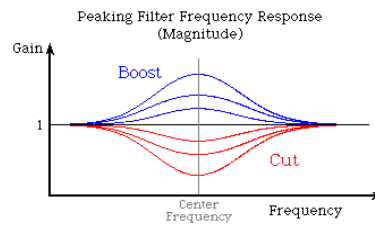
Figure J-DSP simulation using the tone control block.

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## Peaking Filter

In addition to bass and treble controls, peaking filter is designed to boost or cut a small portion of the audio spectrum in “mid” band. The figure below shows frequency response of a peaking filter.



Frequency response of a peaking filter.

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The transfer function of peaking filter is implemented as

$$H(z) = 1 + (\mu - 1) \frac{\alpha(1 - z^{-2})}{0.5 - \gamma \cdot z^{-1} + \beta \cdot z^{-2}}$$

where

$$\beta = \frac{1}{2} \cdot \frac{1 - (4/(1 + \mu)) \tan(\theta_0/2Q)}{1 + (4/(1 + \mu)) \tan(\theta_0/2Q)}$$

$$\gamma = (0.5 + \beta) \cos(\theta_0)$$

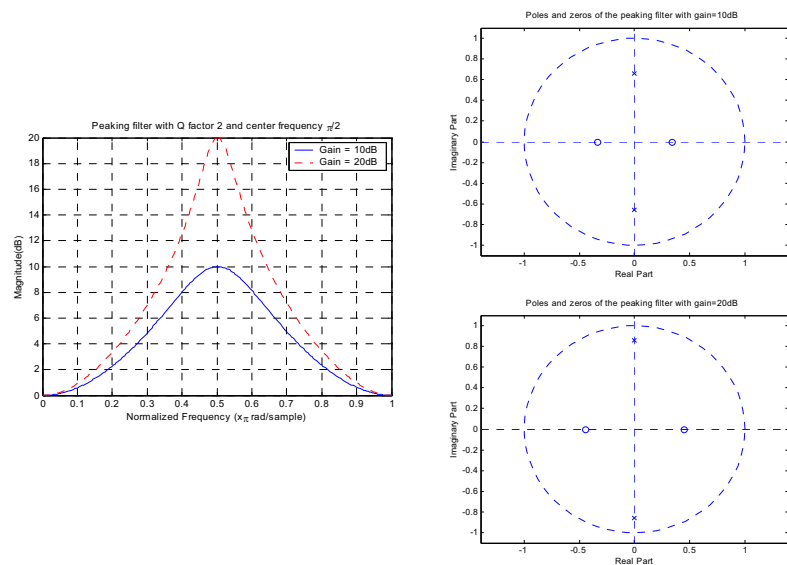
$$\alpha = (0.5 - \beta)/2$$

The poles of peaking filter are calculated by:

$$p_1 = \frac{\cos \theta_0 + \sqrt{(4/(1 + \mu))^2 \tan^2(\theta_0/2Q) - \sin^2 \theta_0}}{1 + (4/(1 + \mu)) \tan(\theta_0/2Q)}, \quad p_2 = \frac{\cos \theta_0 - \sqrt{(4/(1 + \mu))^2 \tan^2(\theta_0/2Q) - \sin^2 \theta_0}}{1 + (4/(1 + \mu)) \tan(\theta_0/2Q)}$$

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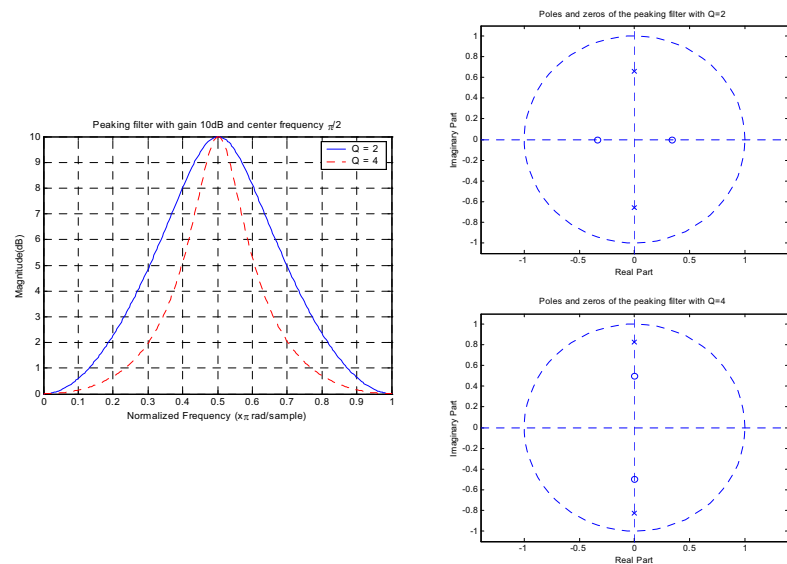
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Frequency response and pole-zero plot of the peaking filter with different gains.

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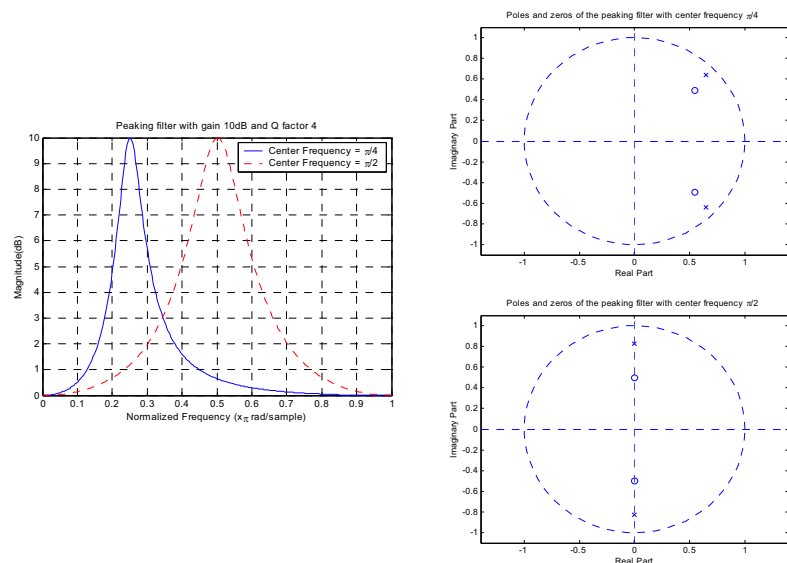
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Frequency response and pole-zero plot of the peaking filter with different Q factors.

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Frequency response and pole-zero plot of the peaking filter with different center frequency. Copyright (c) Andreas Spanias

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## Peaking Filter Block in J-DSP

A J-DSP simulation using the Peaking Filter block is shown below

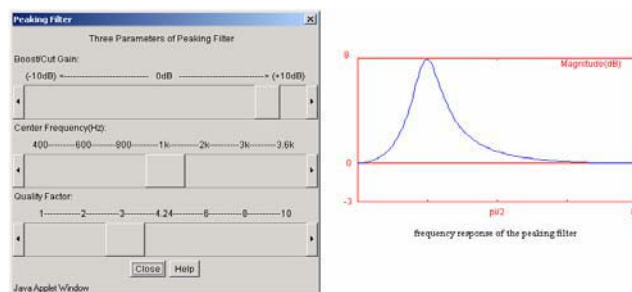


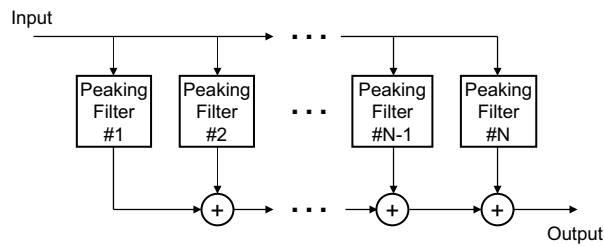
Figure 9: J-DSP simulation using the peaking filter block.

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# Graphic Equalizer

- A graphic equalizer uses a cascade of peaking filters
- It alters the frequency response of each band by varying the corresponding peaking filter's gain.

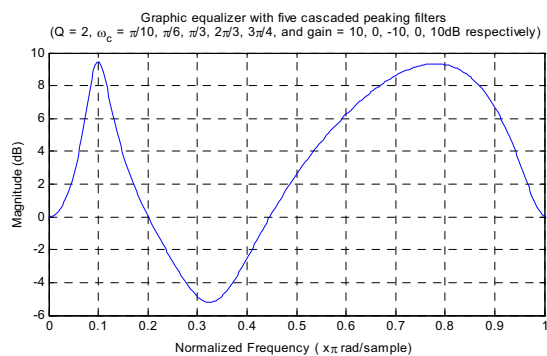


A diagram of a graphic equalizer with N bands of control.

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# MATLAB Simulation



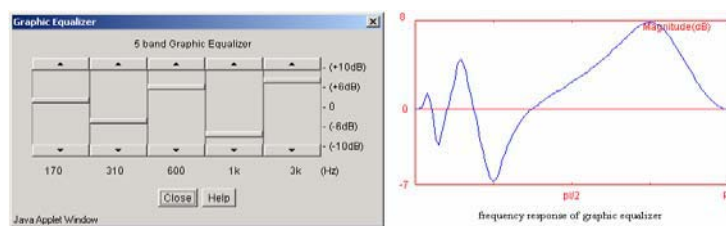
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## Graphic Equalizer Block in J-DSP

A J-DSP simulation using the Graphic Equalizer block is shown below. The sliders are a graphic representation of the frequency response applied to the input audio signal, hence the name “graphic” equalizer.



-DSP simulation using the graphic equalizer block.

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